

6. Gamma Function and Related Functions

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$\Gamma(n+\frac{1}{2}), 8S \quad \ln n - \psi(n), 8D$	
$n=1(1)101$	
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$\log_{10} \Gamma(n+\frac{1}{2}), 8S$	
$n=1(1)101$	

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